

# MATH 466, Spring 2004

## Assignment 1

Due Date: Feb 9

**IMPORTANT NOTE:** A penalty of 30% of total points will be applied to late homework. Write your answers clearly.

1. Do the following problems:

Sec 6.1 : 3(a), 5

Sec 6.2 : 1-4 with 1(a) matrix.

Sec 6.3 : 1(a), 4.

Sec 6.4 : 6, 10.

Sec 6.5 : 3(a), 4(a).

Sec 6.6 : 1, 3 and 5 with 2(a) matrix, 6(c), 11.

2. Show that the Gaussian Elimination with Backward Substitution requires  $\frac{n^3}{3} + n^2 - \frac{n}{3}$  multiplications/divisions, and  $\frac{n^3}{3} + \frac{n^2}{2} - \frac{5n}{6}$  additions/subtractions.
3. Show that  $\det(AB) = \det(A)\det(B)$  for  $n \times n$  matrices  $A$  and  $B$ .
4. (Programming) GEpartialpivot.m is MATLAB code for Gaussian Elimination with partial pivoting. Fill out the backward substitution in GEpartialpivot.m and test it with the following matrix:

$$\begin{bmatrix} 6.0 \times 10^{-7} & 1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$$

Compare this solution with Gaussian Elimination without pivoting, which can be obtained by modifying the same MATLAB code. Which one is correct? Explain why these two solutions are different.